Exhaustivity implicatures and attentive content

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→ He doesn't like red, green.

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- (2) I'm probably asking the wrong person, but of red, green, blue ..., which colours does John like? He likes green and blue. → Not red.

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Outline

- 1. Diagnosis
- 2. Theory
- 3. Results
- 4. Discussion (cancellability)

- (3) a. Of red, green and blue, which colours does John like? b. He likes blue. → He doesn't like red
 - c. He likes blue, or blue and red. → He doesn't like red

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Intuition

(3b) and (3c) differ in their attentive content.

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- (3c) draws attention to the poss. that John likes blue and red.
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Diagnosis

- (3) a. Of red, green and blue, which colours does John like?
 - b. He likes blue. → He doesn't like red
 - c. He likes blue, or blue and red. → He doesn't like red

Intuition

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- (3c) draws attention to the poss. that John likes blue and red.
- (And so does (3a).)
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2. Theory

- 2.1. Translation into logic
- 2.2. Semantics
- 2.3. Pragmatics

- (4) a. Which colours (of red, green and blue) does John like?
 b. He likes blue.
 → He doesn't like red
 - c. He likes blue, or blue and red.

 He doesn't like red

- (4) a. Which colours (of red and blue) does John like? b. He likes blue. → He doesn't like red
 - → He doesn't like red c. He likes blue, or blue and red.

- (4) a. There are colours (among red and blue) that John likes.
 - b. He likes blue.
 - → He doesn't like red
 - c. He likes blue, or blue and red.
- → He doesn't like red

- (4) a. John likes blue, red, or blue and red.
 - b. He likes blue.
 - c. He likes blue, or blue and red.

- → He doesn't like red
- → He doesn't like red

- (4) a. John likes blue, red, or blue and red.
 - b. He likes blue.
 - c. He likes blue, or blue and red.

(4) a. John likes blue, red, or blue and red. $p \lor q \lor (p \land q)$ b. He likes blue. p c. He likes blue, or blue and red. $p \lor (p \land q)$

2.2. Semantics (Roelofsen, 2011)

Possibility: a set of worlds

(a,b)

Possibility: a set of worlds (a,b)

▶ *Proposition*: a set of possibilities $(A, B, [\varphi])$

Possibility: a set of worlds (a, b)

▶ Proposition: a set of possibilities $(A, B, [\varphi])$

• Informative content: $|\varphi| \coloneqq \bigcup [\varphi]$

Possibility: a set of worlds

(a,b)

Proposition: a set of possibilities

 $(A, B, [\varphi])$

• Informative content: $|\varphi| := \bigcup [\varphi]$

(4a)
$$[p \lor q \lor (p \land q)]$$
 (4b) $[p]$

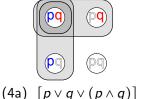
(4c)
$$[p \lor (p \land q)]$$

Possibility: a set of worlds

 $(A, B, \lceil \varphi \rceil)$

(a,b)

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$$(4c) [p \lor (p \land q)]$$

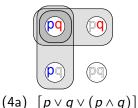
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(4c)
$$[p \lor (p \land q)]$$

Entailment

A entails B, $A \models B$, iff

- (i) $\bigcup A \subseteq \bigcup B$; and
- (ii) for all $b \in B$, if $b \cap \bigcup A \neq \emptyset$, $b \cap \bigcup A \in A$

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$$(4a) [p \lor q \lor (p \land q)]$$

(4b)
$$[p]$$

$$(4c) [p \lor (p \land q)]$$

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A entails B, $A \models B$, iff

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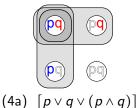
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$$(4c) [p \lor (p \land q)]$$

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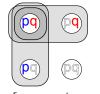
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(4a)
$$[p \lor q \lor (p \land q)]$$

(4b)
$$[p]$$

$$(4c) [p \lor (p \land q)]$$

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A entails B, $A \models B$, iff

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- (ii) for all $b \in B$, if $b \cap \bigcup A \neq \emptyset$, $b \cap \bigcup A \in A$ \longrightarrow at least as attentive

Now, (4c) = (4a), but $(4b) \neq (4a)$.

The relevant maxims

- 1. Quality:
- 2. Quantity:
- 3. Relation:

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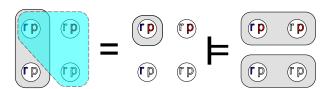
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The relevant maxims

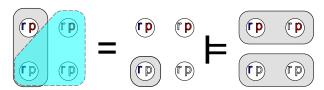
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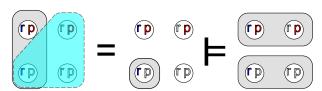
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- 3. **Relation**: $\{r \cap s \mid r \in R\} \models Q$.
- (5) Did John go to the party? It was raining. → If it rained, John {went / didn't go}.



The relevant maxims

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- 2. **Quantity**: For all $Q' \subseteq Q$, if $s \subseteq \bigcup Q'$ then $\bigcup R \subseteq \bigcup Q'$.
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(cf. Grice, 1975; Groenendijk and Stokhof, 1984; Roberts, 1996; Spector, 2007)

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- 3. **Relation**: $\{r \cap s \mid r \in R\} \vDash Q$.

b. He likes blue. (p)

(4) a. John likes blue, red, or blue and red. $(p \lor q \lor (p \land q))$

c. He likes blue, or blue and red. $(p \lor (p \land q))$

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$$(p \lor (p \land q))$$

1.
$$s \subseteq |p \lor (p \land q)|$$

(Quality)

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$$s \subseteq |p \vee (p \wedge q)| = |p|$$

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(Quality)

2. $s \not \equiv |q|$

(Quantity)

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$$(p \lor (p \land q))$$

1. $s \subseteq |p \lor (p \land q)| = |p|$ (Quality)
2. $s \not = |q|$ (Quantity)

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c. He likes blue, or blue and red.
$$(p \lor (p \land q))$$

1. $s \subseteq |p \lor (p \land q)| = |p|$ (Quality)
2. $s \not\equiv |q|$ (Quantity)
3. - $p \lor (p \land q) \models p \lor q \lor (p \land q)$ (Relation)

- (4) a. John likes blue, red, or blue and red. $(p \lor q \lor (p \land q))$
 - b. He likes blue. (p)

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$$s \subseteq |p|$$
 (Quality)

c. He likes blue, or blue and red. $(p \lor (p \land q))$ 1. $s \subseteq |p \lor (p \land q)| = |p|$ (Quality) 2. $s \not\equiv |q|$ (Quantity) 3. - $p \lor (p \land q) \models p \lor q \lor (p \land q)$ (Relation)

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- c. He likes blue, or blue and red. $(p \lor (p \land q))$
 - 1. $s \subseteq |p \vee (p \wedge q)| = |p|$

(Quality)

2. *s* ⊈ |*q*|

 $pv(p \land q) \models pvqv(p \land q)$

(Quantity) (Relation)

3. -

- (4) a. John likes blue, red, or blue and red. $(p \lor q \lor (p \land q))$
 - b. He likes blue. (p)
 - 1. $s \subseteq |p|$ 2. $s \notin |q|$

b \ b^d^(b∨d)

(Quality) (Quantity)

c. He likes blue, or blue and red. $(p \lor (p \land q))$

1. $s \subseteq |p \vee (p \wedge q)| = |p|$

(Quality)

2. s ⊈ |q|

(Quantity)

3. -

 $b \wedge (b \vee d) \models b \wedge d \wedge (b \vee d)$

(Relation)

- (4) a. John likes blue, red, or blue and red. $(p \lor q \lor (p \land q))$
 - b. He likes blue. (p)
 - 1. $s \subseteq |p|$ 2. $s \not \equiv |q|$

 $b \nvDash b \wedge d \wedge (b \vee d)$

(Quality) (Quantity)





- c. He likes blue, or blue and red. $(p \lor (p \land q))$
 - 1. $s \subseteq |p \vee (p \wedge q)| = |p|$

(Quality)

2. $s \notin |q|$

(Quantity)

3. -

 $p_{\lambda}(b \vee d) \models b_{\lambda}(b \vee d)$

(Relation)

- (4) a. John likes blue, red, or blue and red. $(p \lor q \lor (p \land q))$
 - b. He likes blue. (p)
 - 1. $s \subseteq |p|$
 - 2. $s \notin |q|$

$$b \nvDash_{i,i} b \land d \land (b \lor d)$$

(Quality) (Quantity)





- c. He likes blue, or blue and red. $(p \lor (p \land q))$
 - 1. $s \subseteq |p \vee (p \wedge q)| = |p|$

(Quality)

2. s ⊈ |q|

 $pv(p \land q) \models pvqv(p \land q)$

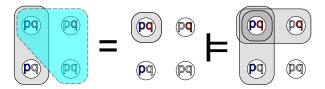
(Quantity)

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 - 1. $s \subseteq |p|$
 - 2. s ⊈ |q|

$$b \nvDash_{iii} b \land d \land (b \lor d)$$

(Quality) (Quantity)



- c. He likes blue, or blue and red. $(p \lor (p \land q))$
 - 1. $s \subseteq |p \vee (p \wedge q)| = |p|$

(Quality)

2. s ⊈ |q|

(Quantity)

3. -

 $b \wedge (b \vee d) \models b \wedge d \wedge (b \vee d)$

(Relation)

- (4) a. John likes blue, red, or blue and red. $(p \lor q \lor (p \land q))$
 - b. He likes blue. (p)
 - 1. $s \subseteq |p|$
 - 2. $s \notin |q|$

$$b \not\models b \land d \land (b \lor d)$$

(Quality) (Quantity)





- c. He likes blue, or blue and red. $(p \lor (p \land q))$
 - 1. $s \subseteq |p \vee (p \wedge q)| = |p|$

(Quality)

2. *s* ⊈ |*q*|

 $pv(p \land q) \models pvqv(p \land q)$

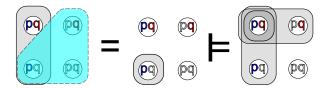
(Quantity)

3. -

(Relation)

- (4) a. John likes blue, red, or blue and red. $(p \lor q \lor (p \land q))$
 - b. He likes blue. (p)
 - 1. $s \subseteq |p|$
 - $b \nvDash b \wedge d \wedge (b \vee d)$ 2. $s \not \equiv |q|$

(Quality) (Quantity)



- c. He likes blue, or blue and red. $(p \lor (p \land q))$
 - 1. $s \subseteq |p \vee (p \wedge q)| = |p|$

(Quality)

- 2. $s \notin |q|$
- $p_{\lambda}(b \vee d) \models b_{\lambda} d_{\lambda}(b \vee d)$

(Quantity)

3. -(Relation)

- (4) a. John likes blue, red, or blue and red. $(p \lor q \lor (p \land q))$
 - b. He likes blue. (p)
 - 1. $s \subseteq |p|$ 2. $s \notin |q|$ $p \not\models p \land q \land (p \land q)$ (Quality) (Quantity)
 - 3. $s \subseteq |\overline{p}| \cup |q| \text{ or } s \subseteq |\overline{p}| \cup |\overline{a}|$ (Relation)

- c. He likes blue, or blue and red. $(p \lor (p \land q))$
 - 1. $s \subseteq |p \vee (p \wedge q)| = |p|$ (Quality) 2. *s* ⊈ |*q*| (Quantity)
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- (4) a. John likes blue, red, or blue and red. $(p \lor q \lor (p \land q))$
 - b. He likes blue. (p)
 - 1. $s \subseteq |p|$ 2. $s \notin |q|$ $p \not\models p \land q \land (p \land q)$ (Quality) (Quantity)
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(Quality)

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3. -

 $b \wedge (b \vee d) \models b \wedge d \wedge (b \vee d)$

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Main conclusion:

- If pragmatic reasoning is sensitive to attentive content (which it must be, to distinguish between (4b) and (4c));
- then exhaustivity is a conversational implicature.

4. Discussion

- 4.1. 'Alternatives'
- 4.2. Cancellability
- 4.3. Semantic desiderata
- 4.4. 'Gricean'?

Existing approaches (since forever):

Why did the speaker not say "p ∧ q"?"

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- Hence something stronger is implied: exhaustivity.

Beware:

- ▶ The 'alternatives' are fully determined by the maxims.
- Speakers need not reason in terms of alternatives.

'If exhaustivity is a conversational implicature, then why is it sometimes mandatory?'

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- (5) On an unrelated note, it was raining.
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4 D > 4 B > 4 E > 4 E > 9 Q G

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Cls in the sense of Grice (1975) cannot be cancelled in this sense:

1. CI is necessary for maintaining the cooperativity assumption.

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 - (i) revoke the cooperativity assumption; or
 - (ii) revise what counted as cooperative.

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- 2. The mutual assumption of cooperativity is necessary for Cl.
- 3. Hence, cancelling CI requires the sp. to retroactively:
 - (i) revoke the cooperativity assumption; or
 - (ii) revise what counted as cooperative.
- 4. The speaker would be either uncooperative, or inconsistent.



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- 'Cancellation' (in the sloppy sense) is not a uniform phenomenon:
 - complete absense of implicature
 - contextual disambiguation
 - correction/inconsistency
 - non-cooperativity

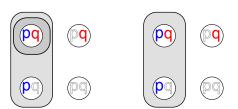
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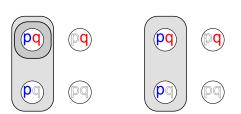
These surely have different cognitive correlates?

▶ No absorption: $p \lor (p \land q) \not\equiv p \not\equiv p \land (p \lor q)$

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- ▶ No absorption: $p \lor (p \land q) \not\equiv p \not\equiv p \land (p \lor q)$
- Questions, the responses to which may be exhaustified, are not partitions.
 (cf. Groenendijk and Stokhof, 1984)



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- Grice wouldn't be against other dimensions of meaning.
- ▶ The connectives are still algebraically 'basic'.

Besides: this is the only way.

The end

Contact

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Articles

- Exhaustivity through the maxim of Relation (LENLS proceedings, see staff.science.uva.nl/~westera/)
- 'Attention, I'm violating a maxim!' (submitted, available through me)

Thanks to the *Netherlands Organisation for Scientific Research* (NWO) for financial support; to F. Roelofsen, J. Groenendijk, C. Cummins, E. Onea, K. von Fintel, the audiences of *SemDial, UCSC S-Circle, SPE6, ICL, ESSLLI StuS, TbiLLC*, Göttingen, and many anonymous reviewers for valuable comments.

Appendix A. Semantics (Roelofsen, 2011)

Ingredients

- Possibility: a set of worlds (a, b)
- *Proposition*: a set of possibilities $(A, B, [\varphi])$
- Informative content: $|\varphi| := \bigcup [\varphi]$
- A restricted to b, $A_b := \{a \cap b \mid a \in A, a \cap b \neq \emptyset\}$

Semantics of relevant fragment

- 1. $[p] = \{ \{ w \in \mathbf{Worlds} \mid w(p) = \mathsf{true} \} \}$
- 2. $[\varphi \lor \psi] = ([\varphi] \cup [\psi])_{|\varphi| \cup |\psi|} = [\varphi] \cup [\psi]$
- 3. $[\varphi \wedge \psi] = ([\varphi] \cup [\psi])_{|\varphi| \cap |\psi|}$

Entailment

A entails B, $A \models B$, iff (i) $\bigcup A \subseteq \bigcup B$ and (ii) $B_{\bigcup A} \subseteq A$.



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- ▶ Roberts's relevance: $R_{CG} \models Q$ (CG = Common Ground)

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Roberts's requirement is too strong:

- ▶ The participants need not *already know* how *R* is relevant.
- They need only be able to figure it out.

E.g., in case of exhaustivity:

- 1. $s \subseteq |p|$ (Quality)
- 2. $s \notin |q|$ (Quantity)
- 3. $s \subseteq \overline{|p|} \cup |q|$ or $s \subseteq \overline{|p|} \cup \overline{|q|}$ (Relation)
- 4. $s \subseteq \overline{|q|}$

Chierchia, et al. (2008), and much subsequent discussion

(10) Which books did every student read? Every student read O. or K.L. → No student read both.

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The 'embedded' implicature of (5) is in fact predicted.



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